

Joint Center for Satellite Data Assimilation Seminar

June 4, 2013

NCWCP, College Park, MD

# Extracting maximum information from GOES-R ABI and GLM instruments in regional data assimilation applications to high-impact weather

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[<https://www.cira.colostate.edu/projects/ensemble/index.php>]

# Contributions and collaborations

## **Programs:**

- GOES-R Risk Reduction
- JCSDA
- NASA Global Precipitation Mission (GPM)
- NSF Collaboration in Mathematical Geosciences (CMG)

## **People:**

- Karina Apodaca (CIRA), Man Zhang (CIRA), Lous Grasso (CIRA), Mark DeMaria (NOAA/STAR), John Knaff (NOAA/STAR), Min-Jeong Kim (CIRA-NOAA/EMC)
- Jun Li (CIMSS, Univ. Wisconsin)
- Prof. I. M. Navon (Florida State University)
- Sara Zhang (NASA/GSFC), Arthur Hou (NASA/GSFC)

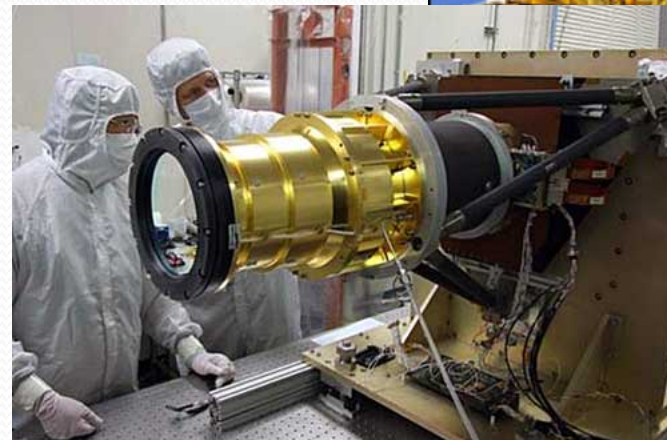
## **High-End Computing:**

- NOAA S4 (SSEC, Univ. Wisconsin)
- NCAR CISL (Bluefire, Yellowstone)
- NASA (Pleiades)

# Motivation-1: GOES-R Satellite

- **Geostationary Operational Environmental Satellite**

- ❑ Advanced Baseline Imager (ABI)
  - ✧ 16 spectral bands (Vis/WV/IR)
  - ✧ Resolution: 5-15 min, 0.5-2 km
- ❑ Geostationary Lightning Mapper (GLM)
  - ✧ Total lightning (in-cloud, cloud-to-ground)
  - ✧ Day and night detection
  - ✧ Resolution: 8 -14 km
- ❑ High-impact weather
- ❑ Precipitation (water vapor, clouds)
- ❑ Air pollution (dust, SO<sub>2</sub>, O<sub>3</sub>)
- ❑ Increased spatiotemporal resolution



# Motivation-2: High-impact weather

- **Severe weather**

- ✧ Thunderstorms
- ✧ Tornadoes
- ✧ Rainfall
- ✧ Hail
- ✧ Flash floods



Mississippi tornado (04/2011)

- **Tropical cyclones**

- ✧ High winds
- ✧ Storm surge
- ✧ Rainfall
- ✧ Floods
- ✧ Tornadoes
- ✧ Rip currents



Hurricane Andrew (1992) - wind damage

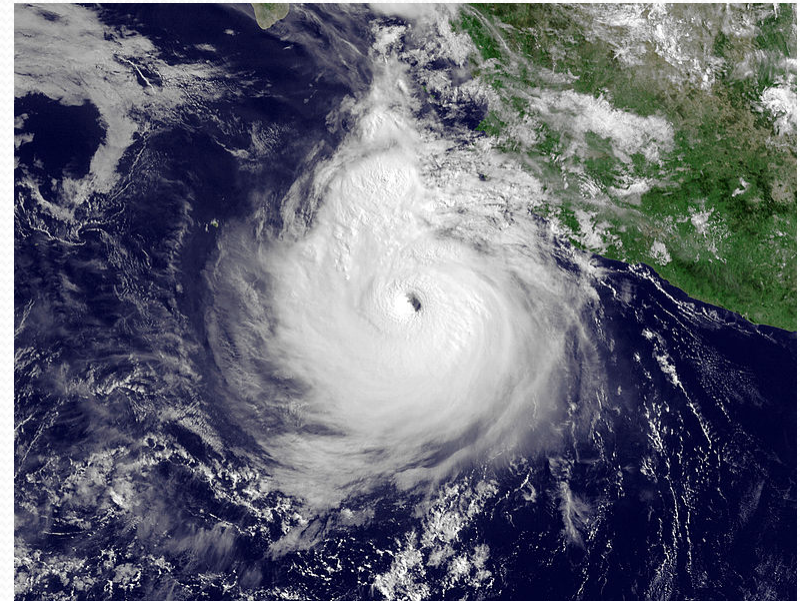


## Motivation-2: High-impact weather

- **Clouds: information to be utilized**
  - ✧ Typically associated with high impact weather
  - ✧ Can produce extreme rainfall and floods
  - ✧ High spatiotemporal resolution (microphysics)
  - ✧ Radiation



Supercell thunderstorm cloud (2010) - NASA



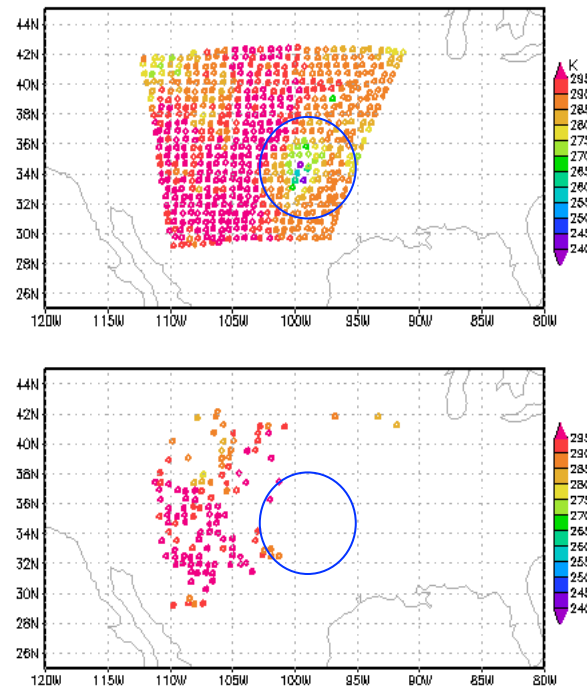
Hurricane Dora (2012) - GOES

**Improving analysis and prediction of clouds is challenging, but fundamentally important**

# Motivation-3: All-sky satellite radiance assimilation

- **Satellites observe clouds**
  - ✧ Visible, Water-vapor, Infrared, Microwave
- **Prediction of high impact weather relies on resolving cloud processes**
  - ✧ Cloud microphysics
  - ✧ Precipitation
- **Current operational weather prediction mostly relies on clear-sky radiance assimilation**
  - ✧ Simpler algorithm, computationally efficient
- **Observation of clouds can bring new information relevant for high-impact weather**
  - ✧ Constrain microphysics
  - ✧ Improved cloud representation benefits precipitation and radiation processes
  - ✧ Warn-on-forecast
  - ✧ TC track and intensity

# Impact of cloud clearing



Re-development of the TS Erin (2007): Distribution of AMSU-B radiance data in the NCEP operational data stream: (a) all observations, (b) accepted observations after cloud clearing. Data are collected during the period 15-18Z, August 18, 2007. Note that almost all observations in the area of the storm got rejected by cloud clearing. (from Zupanski et al. 2011, *J. Hydrometeorology*)

**Valuable information is lost due to cloud clearing**

# Satellite observations that can bring new information for high-impact weather

- **Microwave radiances**
  - penetrate clouds, can “see” inside
  - potential benefit for improving intensity of storms
- **Infrared radiances**
  - imager cannot penetrate clouds, can “see” cloud tops
  - potential benefit for improving location of the storm
- **Spaceborne lightning**
  - indirect measurement of weather activity
  - location and intensity of storms
- **Spaceborne radars**
  - can penetrate clouds
  - high resolution

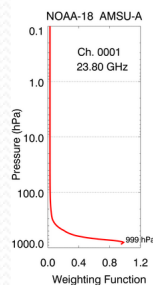
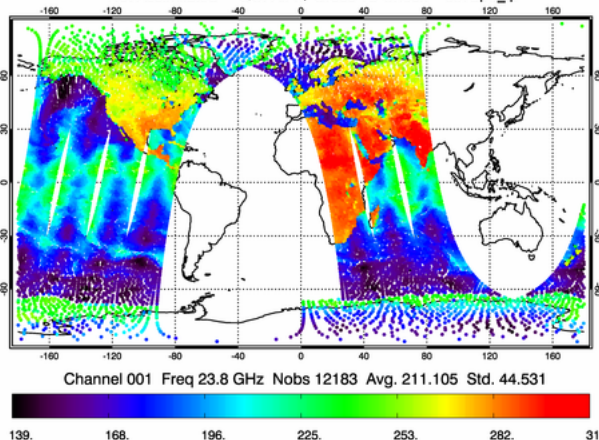


# Microwave satellite information: AMSU-A

Channel 1: **23.8 GHz**

20 May 2013, 12z

Brightness Temperature (K) NOAA-18 AMSU-A 20130520\_12z  
 \*\* Not Assimilated QC: All w/ Gross Tb Check e572p5\_fp

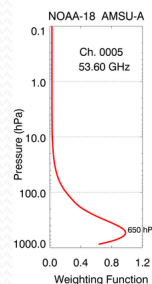
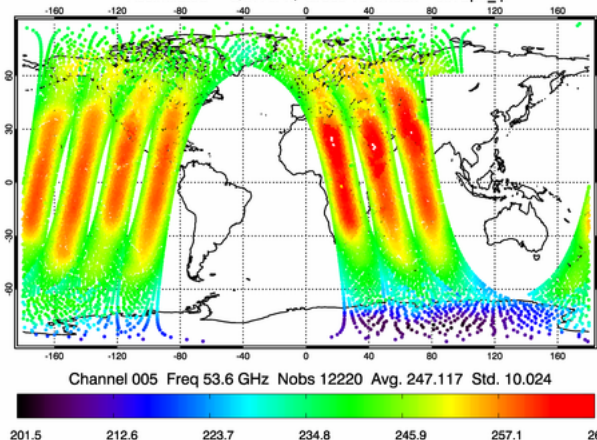


Weighting function: **Surface**

Channel 3: **53.6 GHz**

20 May 2013, 12z

Brightness Temperature (K) NOAA-18 AMSU-A 20130520\_12z  
 \*\* Assimilated QC: All w/ Gross Tb Check e572p5\_fp

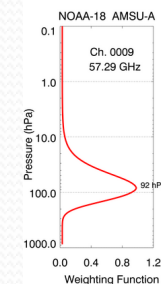
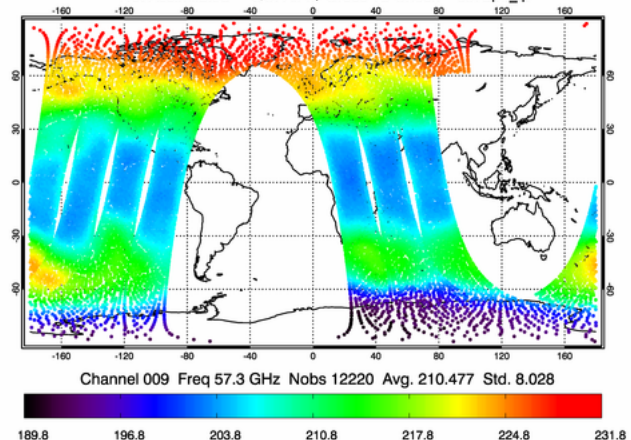


Weighting function: **650 hPa**

Channel 9: **57.3 GHz**

20 May 2013, 12z

Brightness Temperature (K) NOAA-18 AMSU-A 20130520\_12z  
 \*\* Not Assimilated QC: All w/ Gross Tb Check e572p5\_fp



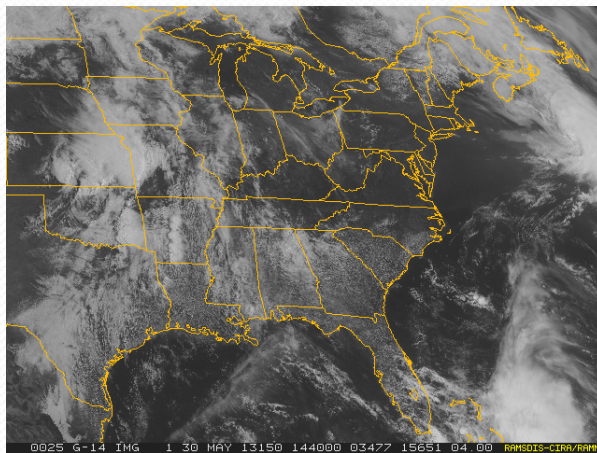
Weighting function: **92 hPa**

**Complementary information from surface, lower and upper troposphere**

# Infrared satellite information: GOES-East

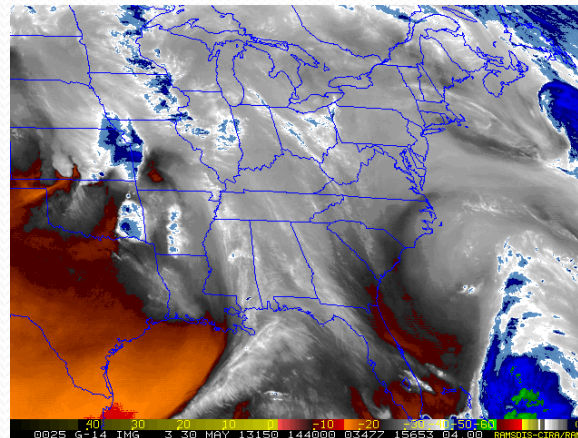
## Visible (4 km)

30 May 2013, 13:15z



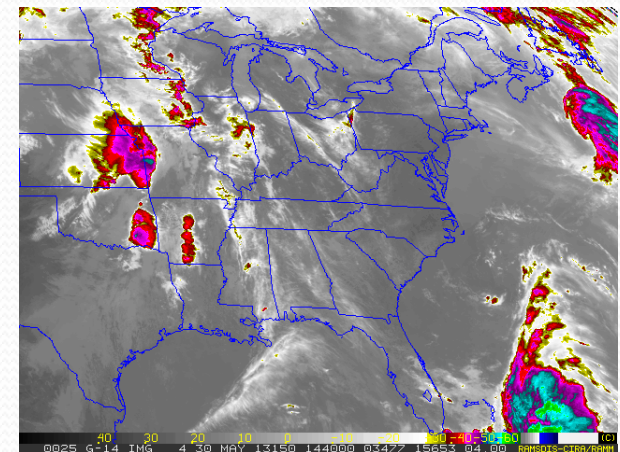
## Water vapor (4 km)

30 May 2013, 13:15z



## Thermal infrared (4 km)

30 May 2013, 13:15z



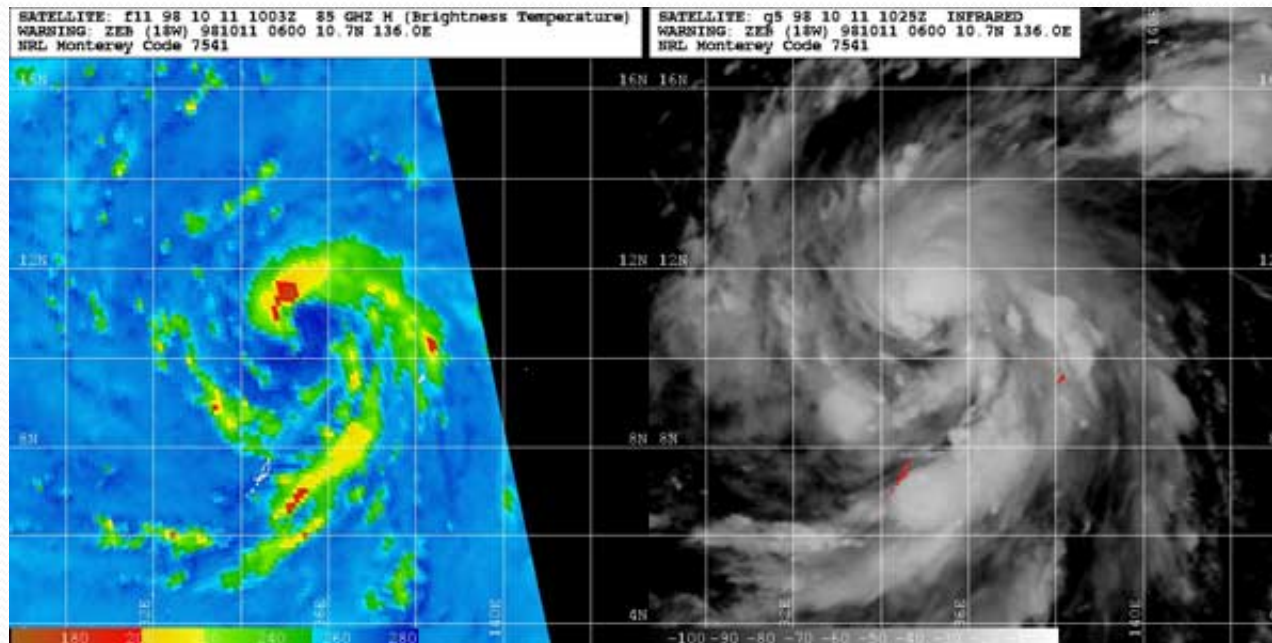
Additional information from multiple channels

# Combined infrared and microwave



MW

IR



Typhoon Zeb (1998):

(**MW**) Dark blue marks a developing eye at the center of circulation. The greens and yellows in the spiral bands represent scattering signatures from precipitation-size ice particles above the freezing level.

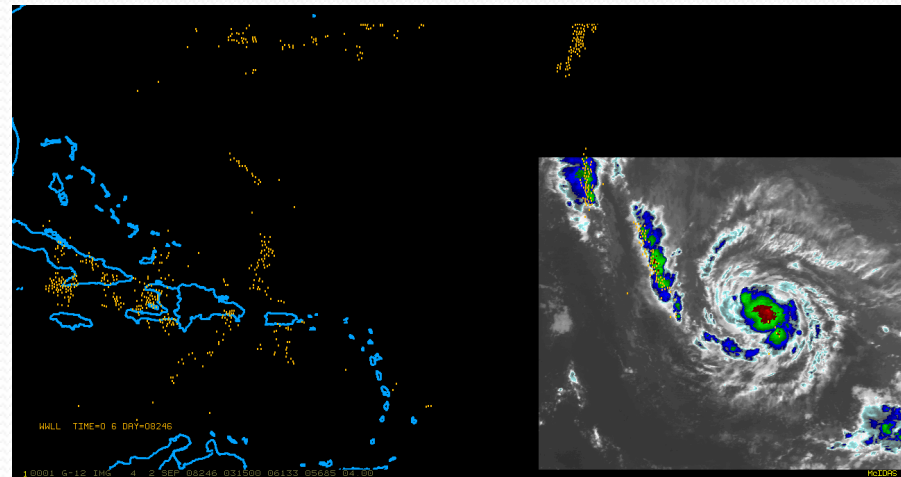
(**IR**) Shows the Cirrus clouds and cumulonimbus that covers most of the storm. It shows a portion of the eye. However, the northern part of the eye is covered by cirrus clouds.

[Navy Research Lab Monterey, Marine Meteorology Division].

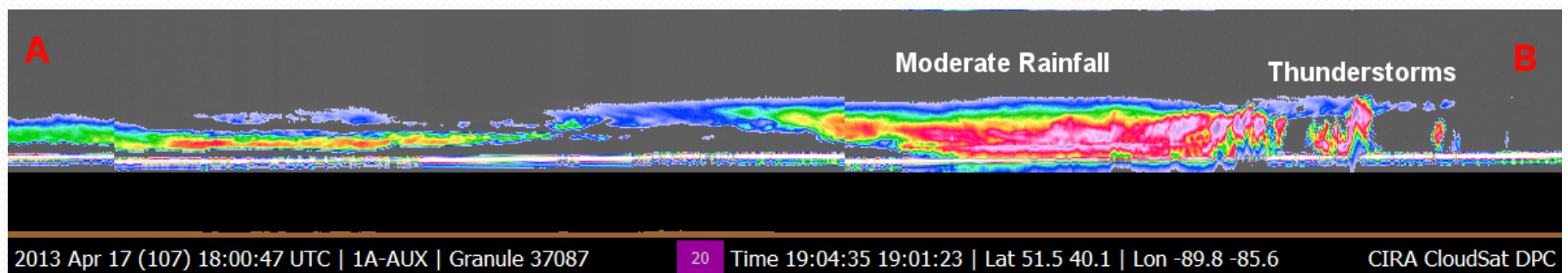


# Lightning and radars

**Lightning:**  
Hurricane Ike (2008)



**CloudSat radar: Chicago flooding (April 2013)**



Detailed information about the storm, clouds, and precipitation



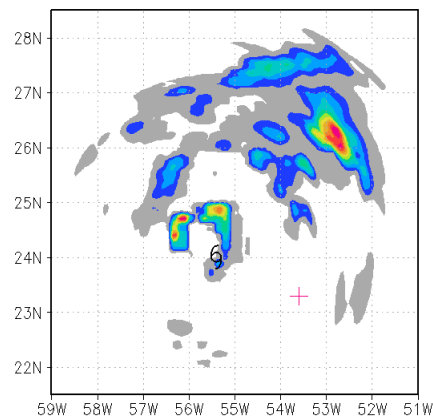
# Challenges of all-sky satellite radiance assimilation for high-impact weather

- **Nonlinearity and non-differentiability**
  - ✧ Microphysical processes
  - ✧ Radiative Transfer (RT) model
- **Forecast error covariance**
  - ✧ Flow-dependent, cross-variable correlations, microphysics, dynamics
- **Bias correction**
  - ✧ Predictors for cloudy radiance bias correction
- **Computational limitations**
  - ✧ High-dimensional state vector for cloud-resolving data assimilation
  - ✧ Additional RT model calculations (e.g., scattering)
- **Other relevant issues**
  - ✧ Correlated observation errors
  - ✧ Non-Gaussian errors

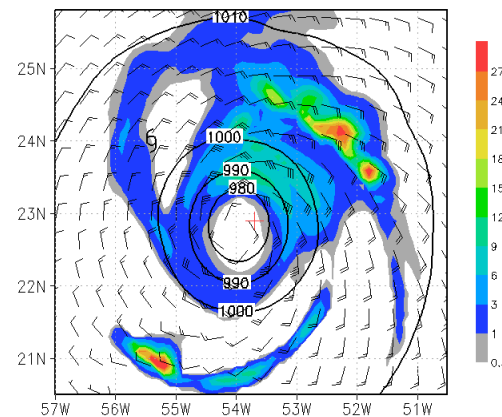
# Nonlinearity: Impact of minimization in all-sky MW radiance DA: Hurricane Danielle (2010)

- Assimilation of AMSU-A all-sky radiances with NOAA HWRF-MLEF (9 km)
- TC circulation represented by total cloud condensate (g/kg)
- Solid lines represent the MSLP (hPa)
- DA cycle 8 valid 1200 UTC 26 August 2010

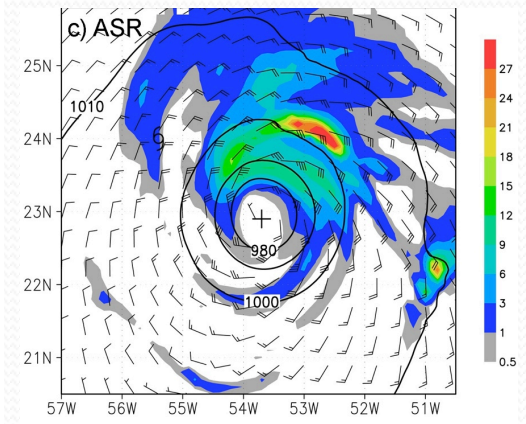
Precipitation rate (mm/h)  
at 1311 UTC 26 Aug 2010



**One** minimization iteration



**Two** minimization iterations



(from M. Zhang et al. 2013, *Mon. Wea. Rev.*)

**Additional minimization iterations may be beneficial**

# Forecast error covariance

$$P_f = \begin{bmatrix} P_{dd} & P_{dc} \\ P_{dc}^T & P_{cc} \end{bmatrix}$$

$P_{dd}$ : Correlations between **dynamical** variables

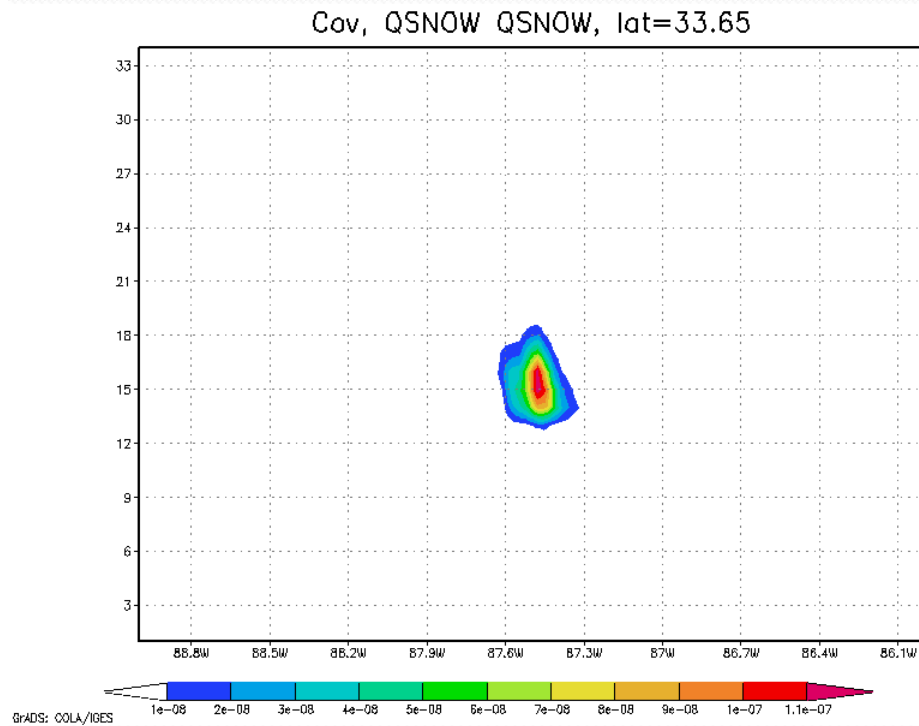
$P_{cc}$ : Correlations between **cloud** (microphysical) variables

$P_{dc}$ : Cross-correlations between **dynamical** and **cloud** variables

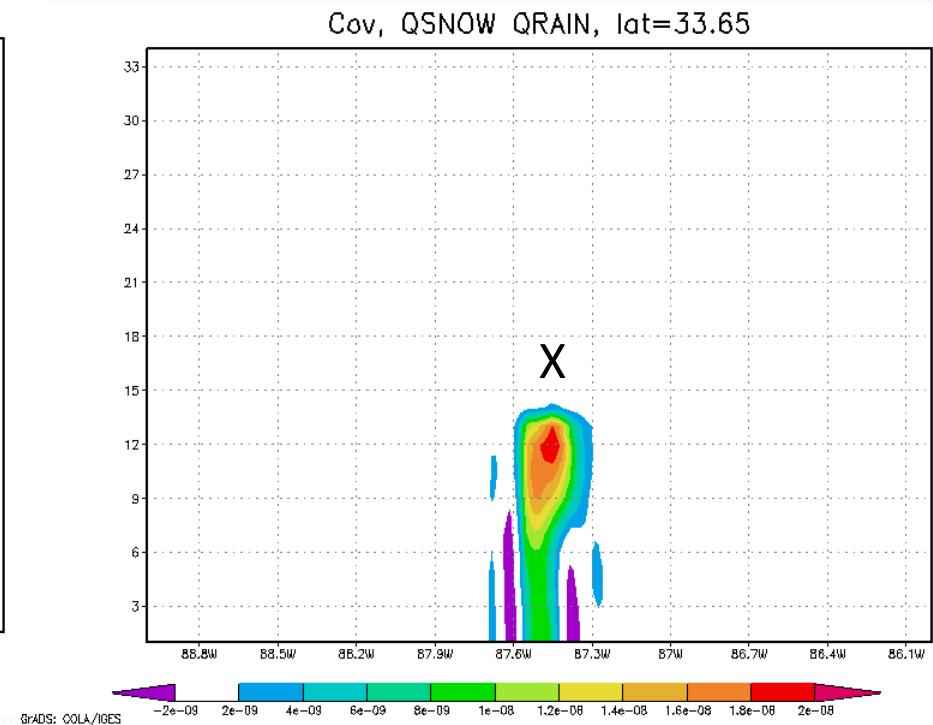
- Only  $P_{dd}$  is well known
- Correlations between microphysical variables not well known
- Even less known correlations between dynamical and microphysical variables

# Single observation of cloud snow at 650 hPa: Vertical response

**(a) Cloud snow at 34N**



**(b) Cloud rain at 34N**



**Flow-dependent and non-centered responses have to be created**



# Data assimilation algorithm: Maximum Likelihood Ensemble Filter (MLEF)



- A hybrid between EnKF and variational methods
  - iterative minimization (variational)
  - multiple realizations of model and observation operators for uncertainty (ensemble)
- Full-rank or reduced-rank
- Deterministic first guess forecast
- Analysis is the maximum of a posterior probability density function
- Nonlinear analysis solution by an iterative minimization
- Improved minimization efficiency by an implicit Hessian preconditioning

## ***References:***

Zupanski 2005 (*MWR*)

Zupanski et al. 2008 (*QJRM*)

# Generalization of Kalman Filter to include nonlinear model operators: MLEF Forecast

$$P_f^{1/2} = MP_a^{1/2} \quad \Rightarrow \quad [p_1^f \quad p_2^f \quad \cdots \quad p_n^f] = [Mp_1^a \quad Mp_2^a \quad \cdots \quad Mp_n^a]$$

- In KF, the forecast error column is a forecast of the analysis error column
- Since  $\{p_1^a \quad p_2^a \quad \cdots \quad p_n^a\}$  spans the analysis uncertainty subspace, one can say that uncertainty is transported in time by a linear model  $M$

**Generalize KF to include nonlinear forecast model:**

**Transport uncertainty in time by a *nonlinear* model  $\mathcal{M}$**

$$x^f = \mathcal{M}(x^a) \quad x_i^f = \mathcal{M}(x^a + p_i^a)$$

$$p_i^f = x_i^f - x^f = \mathcal{M}(x^a + p_i^a) - \mathcal{M}(x^a)$$

# Generalization of Kalman Filter to include nonlinear observation operators: MLEF Analysis

In standard KF, the analysis is obtained by minimizing a quadratic cost function (i.e. linear observation operators)

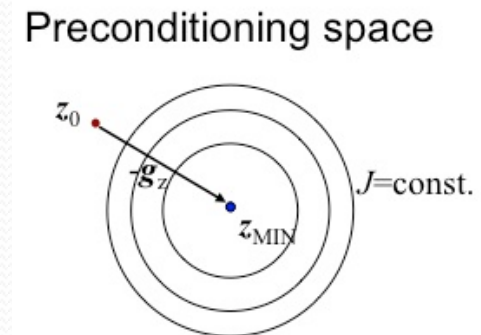
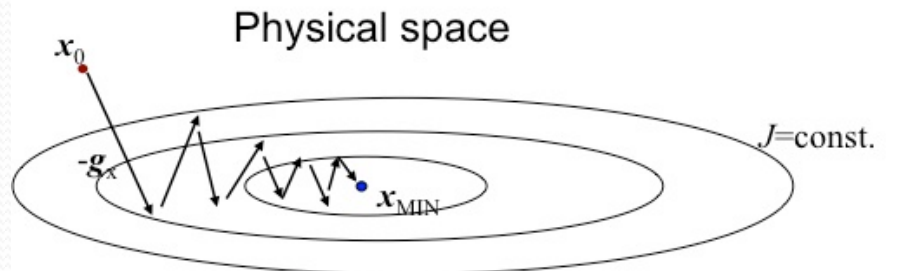
**Generalize KF to include *nonlinear observation operators*:**

- Nonlinear observation operators require a robust and sophisticated minimization, so use the best applicable minimization method
- Since the minimization is critical, build data assimilation around minimization

$$J(x) = \frac{1}{2} \left( x - x^f \right)^T P_f^{-1} \left( x - x^f \right) + \frac{1}{2} \left( y - \mathcal{K}(x) \right)^T R^{-1} \left( y - \mathcal{K}(x) \right)$$

# Why is Hessian preconditioning important?

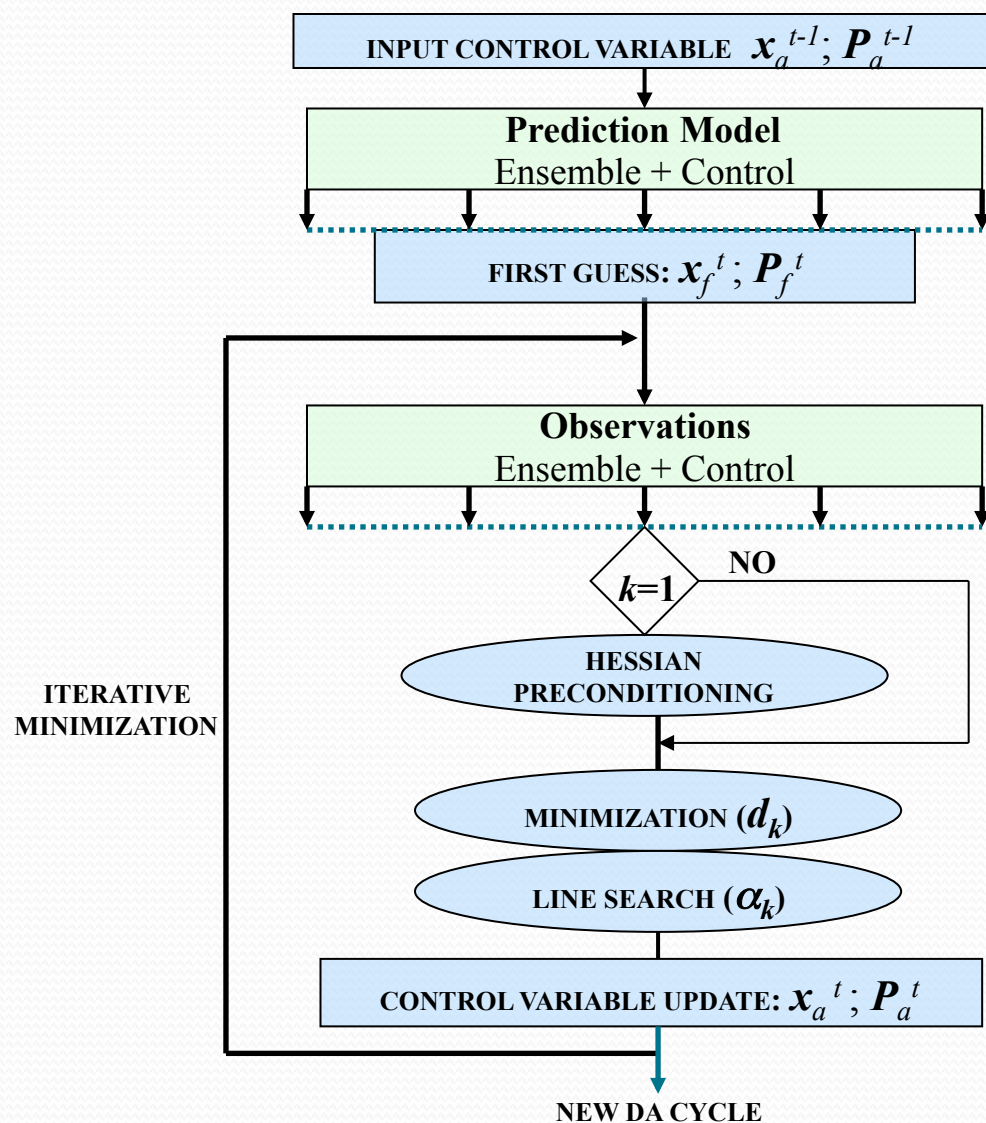
$$x - x_f = P_f^{1/2} (I + P_f^{T/2} K^T R^{-1} K P_f^{1/2})^{-1/2} z$$



- ☐ Fast convergence from arbitrary initial state
- ☐ Impacts dynamical balance in multivariate DA



# MLEF flowchart



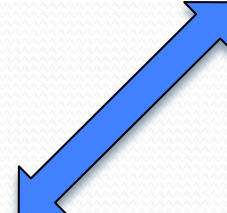
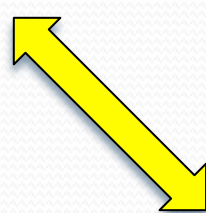
# Modular MLEF

## Observation module:

- Transform/interpolate from model to observations
- Read observations
- Output observation info: increments, errors, ...

## Forecast module:

- Import the forecasting system with pre- and post-processing
- Make *namelist.input* on-the-fly



## Data assimilation module:

- Controls the processing of the model and observation info
- Hessian preconditioning, gradient, minimization iterations
- State vector and uncertainty estimates

# Quantifying satellite information using Shannon information measures

## Entropy

$$H\{X\} = -\int p(x) \log(p(x)) dx$$

## Change of entropy due to observations

$$\Delta H = H\{X\} - H\{X|Y\}$$

- Gaussian pdf greatly reduce the complexity since entropy is related to covariance

Change of entropy / degrees of freedom for signal (DFS)

$$\Delta H = DFS = \text{trace}[I - P_a P_f^{-1}]$$

In ensemble DA methods  $DFS$  can be computed exactly in ensemble subspace:

$$DFS = \text{trace}[(I + Z^T Z)^{-1} Z^T Z] \quad Z = R^{-1/2} H P_f^{1/2} \quad DFS = \sum_i \frac{\lambda_i^2}{1 + \lambda_i^2}$$

**Since eigenvalues of the matrix  $Z^T Z$  are a by-product of assimilation, the flow-dependent  $DFS$  can be computed**

# All-sky microwave radiance assimilation: Tropical Cyclone Core applications

- **Model:** NOAA HWRF (operational in 2011, 27km/9km)
- **Results for TC core area (inner nest) at 9 km resolution**
- **Observations:** AMSU-A all-sky radiances, Channels 1-9 and 15 assimilated
- **Data assimilation interval:** 6 hours
- **Number of ensembles:** 32
- **Hurricane Daniele (2010)**
- **Bias correction from clear-sky GSI output**
- **From M. Zhang et al. (2013, *Mon. Wea. Rev.*)**



# Radiance bias correction and quality control

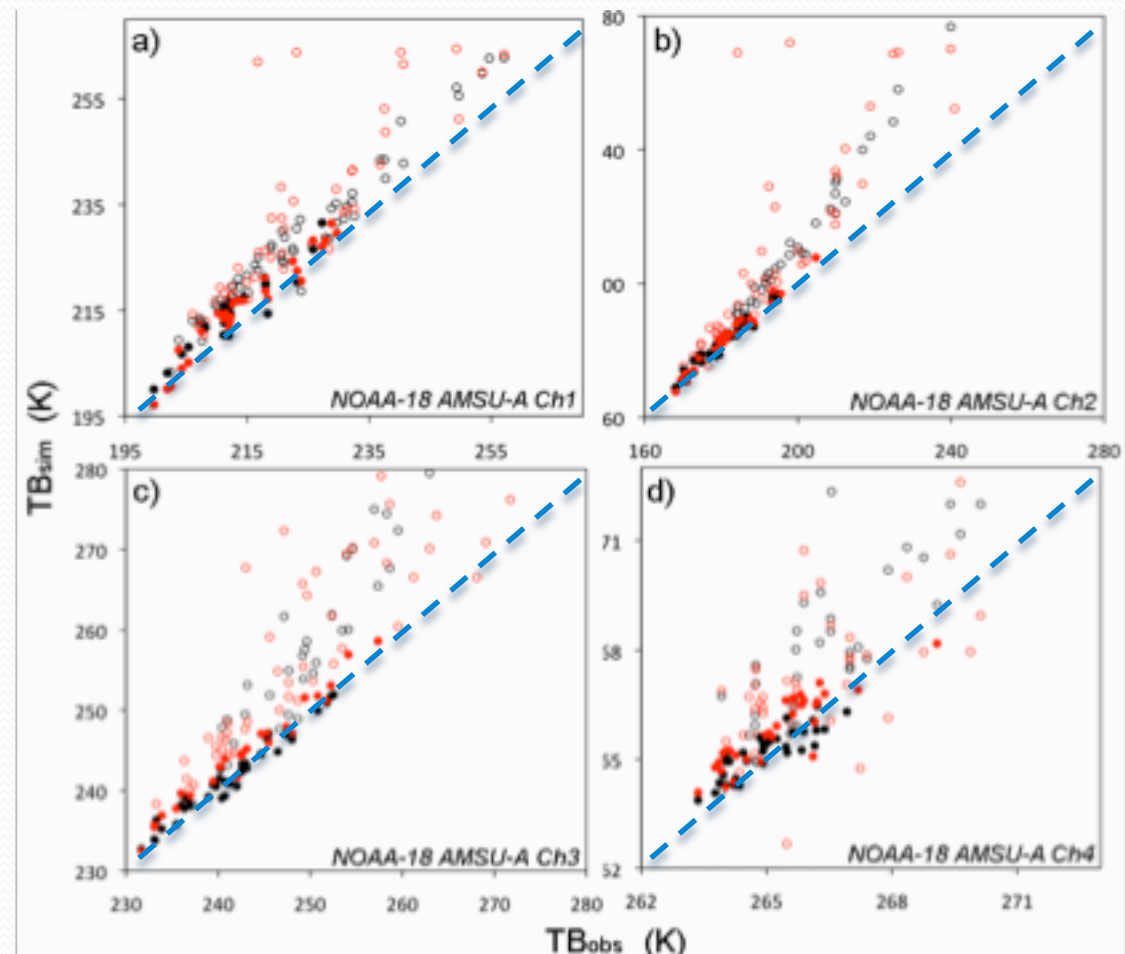
CSR – clear-sky radiance  
ASR – all-sky radiance

**Before quality control and bias correction:**

- red circle: input ASR
- black circle: input CSR

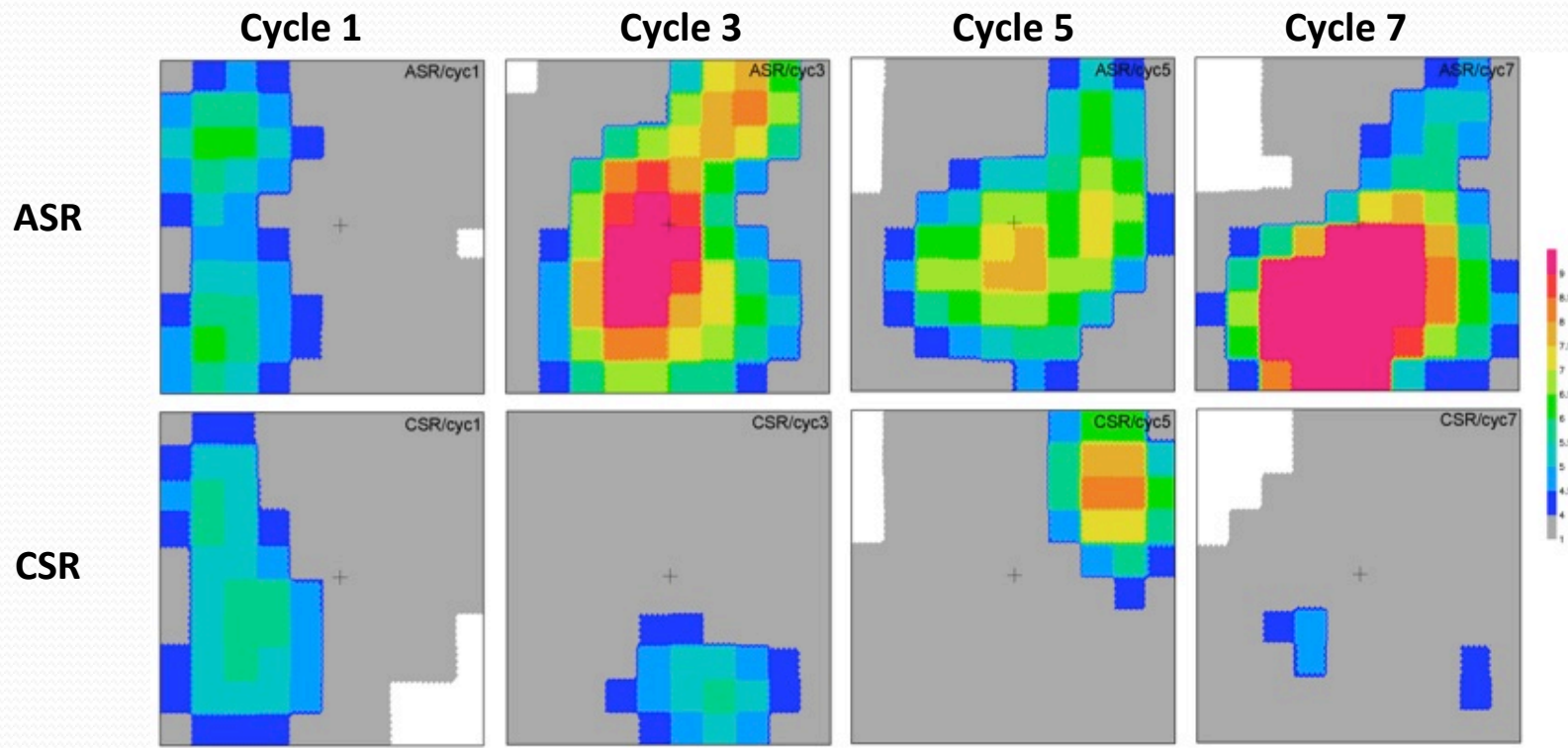
**After quality control and bias correction:**

- Red dot: assimilated ASR
- Black dot: assimilated CSR



Comparable TBs statistics after radiance bias correction and quality control

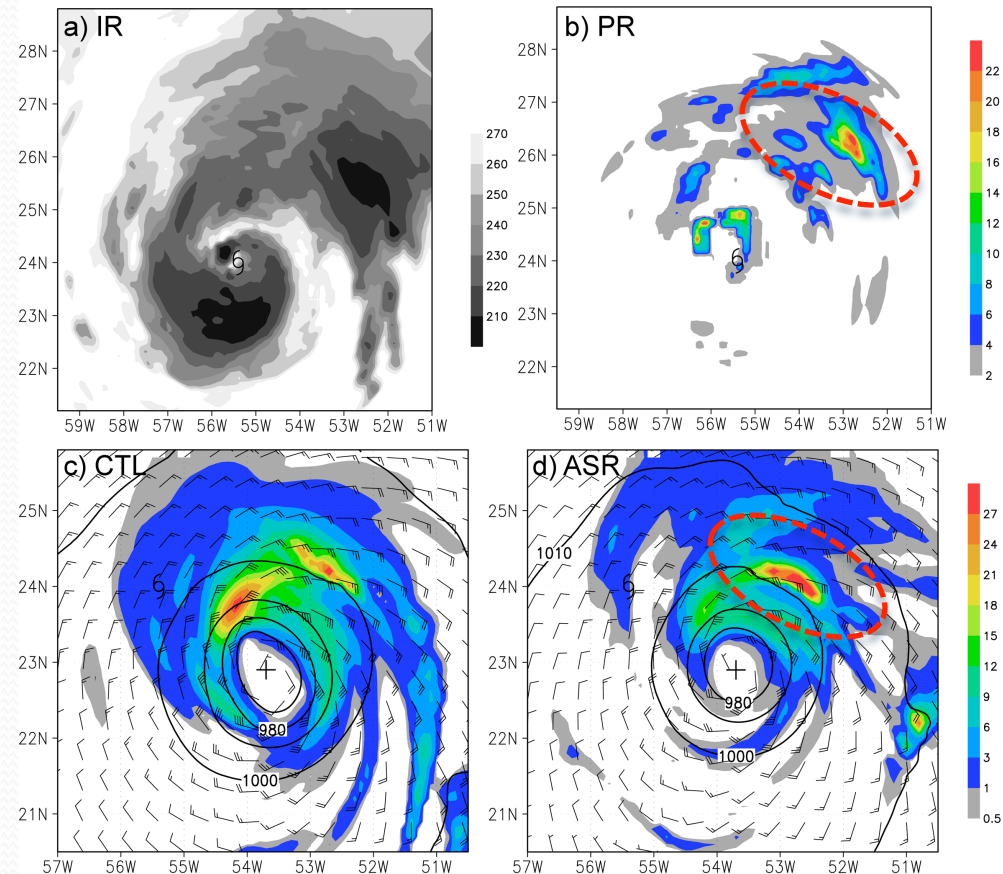
# Hurricane Danielle (2010): All-sky AMSU-A information content (DFS)



Cloudy radiance observations add new information throughout the hurricane development

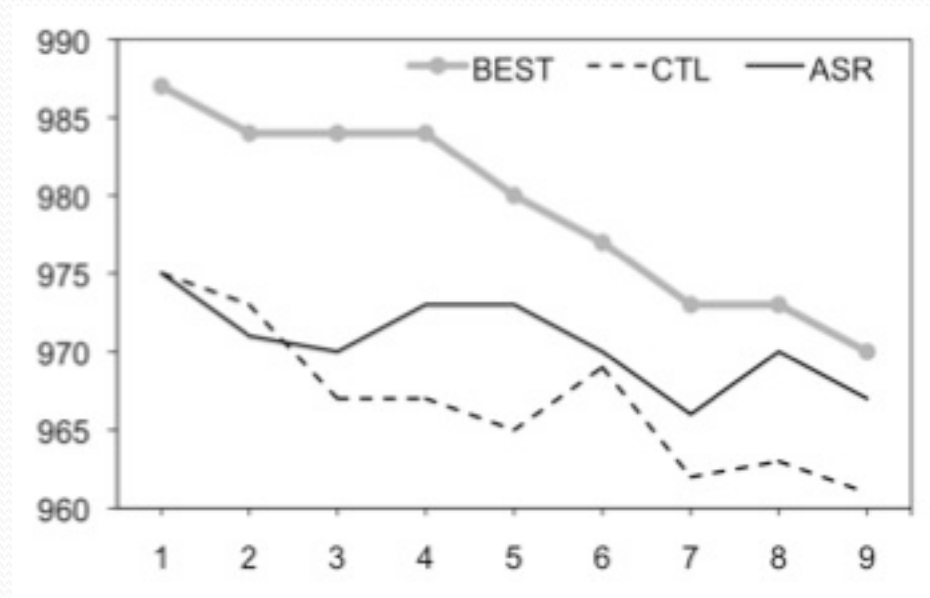
# Hurricane Danielle (2010)

- (a) IR imagery
- (b) AMSU-A retrieved precipitation rate
- (c) CTL – control experiment
- (d) ASR – all-sky experiment



(a) Enhanced Infrared (IR) Imagery at 1145 UTC 26 Aug 2010 (Unit: K); (b) AMSU-retrieved precipitation rate map from MetOp-A at 1311 UTC 26 Aug 2010 (Unit: mm h<sup>-1</sup>). Distribution of the **6-h forecast** of the total cloud condensate (Colored; Unit: Kg m<sup>-2</sup>) at DA cycle 8: (c) the CTL experiment, and (d) the ASR experiment, superposed with mean sea-level pressure and 10-m above ground wind barbs from, valid at 1200 UTC 26 Aug 2010.

# Hurricane Danielle (2010): Intensity



Hurricane Danielle (2010): Time series of the minimum sea level pressure (hPa) for NHC best track data (thick grey line) and MLEF-HWRF experiments ASR (solid) and CSR (dashed) between 1800 UTC 24 Aug and 1800 UTC 26 Aug 2010.

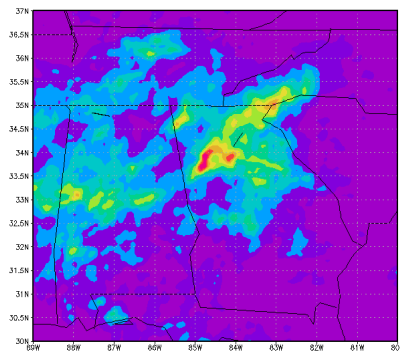
# All-sky microwave radiance assimilation:

## NASA Global Precipitation Mission - GPM: Downscaling satellite precipitation information using ensemble data assimilation (with Sara Zhang and Arthur Hou, NASA GSFC)

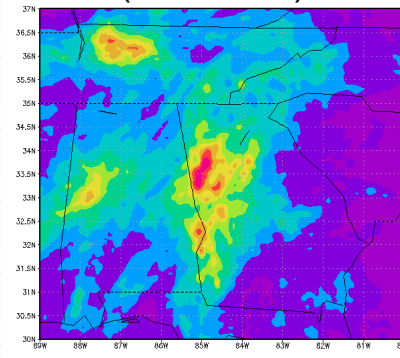
- Provide improved precipitation information for hydrology models
- Cloud-scale data assimilation with NASA WRF model (27-9-3 km)
- From S. Zhang et al. (2012, *Mon. Wea. Rev.*)

### Surface precipitation short-term forecasts verification (accumulated during 15-22 Sep 2009 in the southeast US flood region)

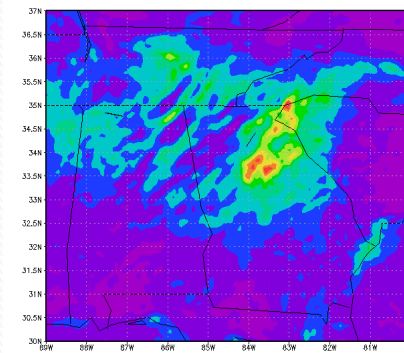
Ground-based Verification  
(NOAA Stage IV data)



3DVAR, no AMSR-E, TMI  
(WRF-GSI)



EDAS, with AMSR-E, TMI  
(WRF-EDAS)





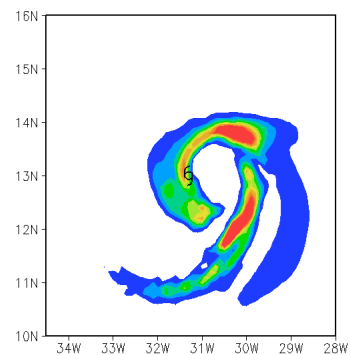
# All-sky infrared radiance assimilation: Tropical Cyclone Core applications

- **Model:** NOAA HWRF (operational in 2011, 27km/9km)
- **Results for TC core area (inner nest) at 9 km resolution**
- **Observations:** SEVIRI all-sky radiances [ $10.8\ \mu\text{m}$  - proxy for GOES-R ABI)
- **Data assimilation interval:** 1 hour
- **Number of ensembles:** 32
- **Hurricane Fred (2009)**
- **No bias correction** (advantage of clear-sky GSI correction not obvious)
- To be submitted for publication by M. Zhang et al.

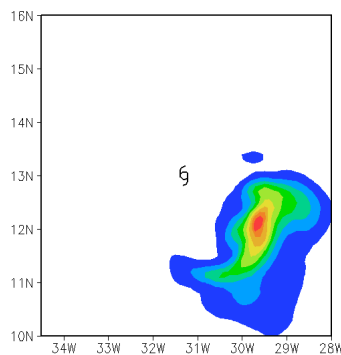
# Hurricane Fred (2009): Analysis

**Total cloud condensate (cwm)**  
Valid 0600 UTC 9 Sep 2009

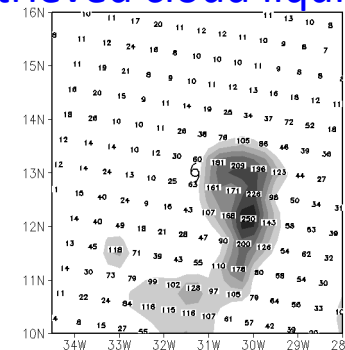
Control experiment



All-sky radiance assimilation



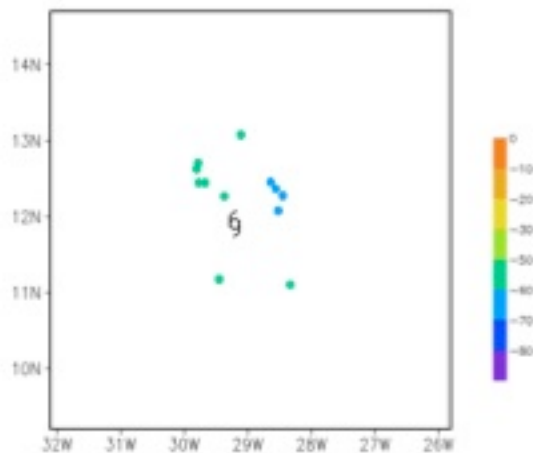
Verification: AMSU-A NOAA-16  
retrieved cloud liquid water



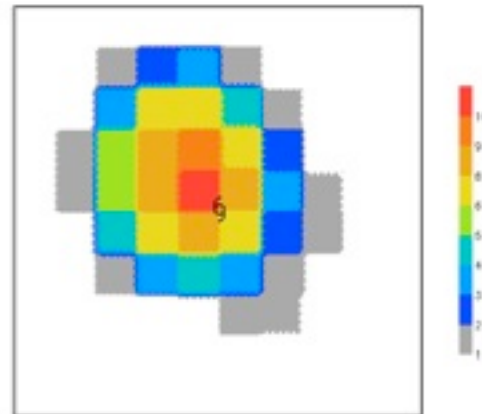
**Assimilation of all-sky infrared radiance is able to improve clouds in TC core**

# Hurricane Fred (2009): All-sky SEVIRI information content (DFS)

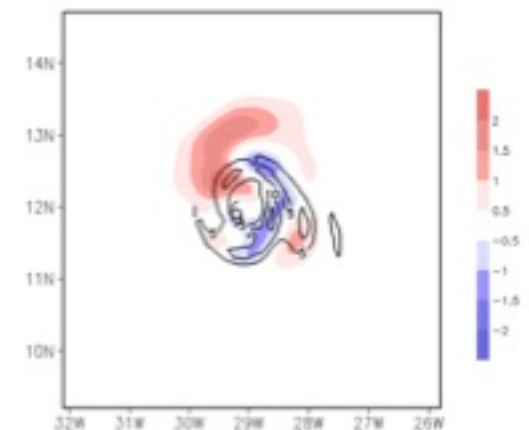
**Tb observations**



**Degrees of  
Freedom for Signal**



**Total cloud  
condensate (cwm)**



**Valid 1800 UTC 08 Sep 2009**

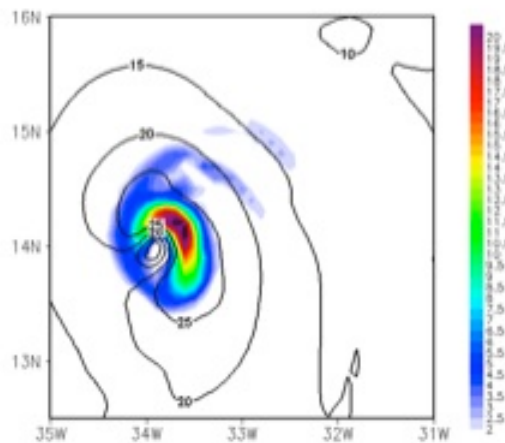
SEVIRI infrared cloudy radiance observations adds new information

# Hurricane Fred (2009): 21-hour forecast

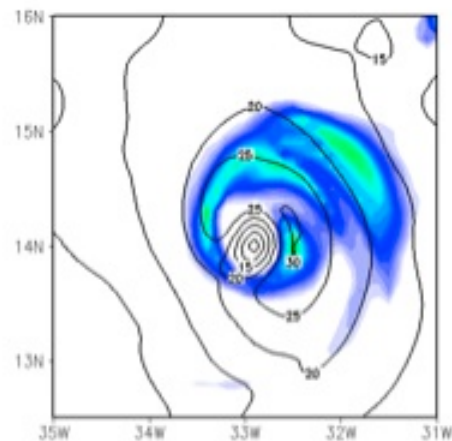
**Total cloud condensate (cwm)**

Valid 0300 UTC 10 Sep 2009

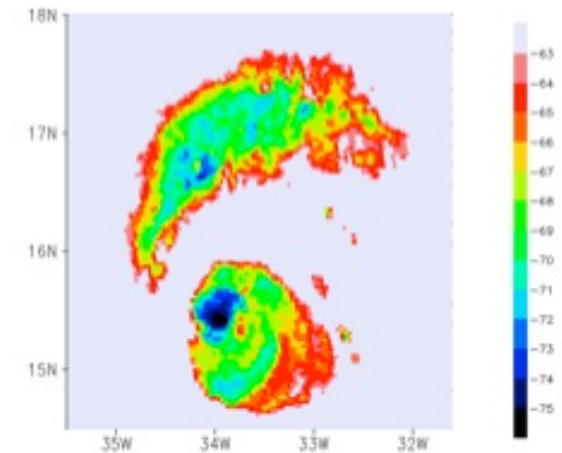
Control experiment



All-sky radiance assimilation



Verification: Seviri  
radiance observations

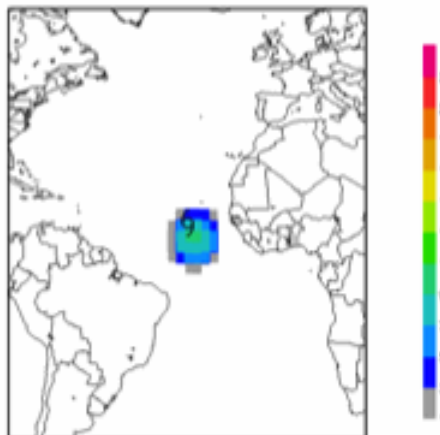


**Assimilation of all-sky infrared radiance improves the forecast of clouds in TC core area**

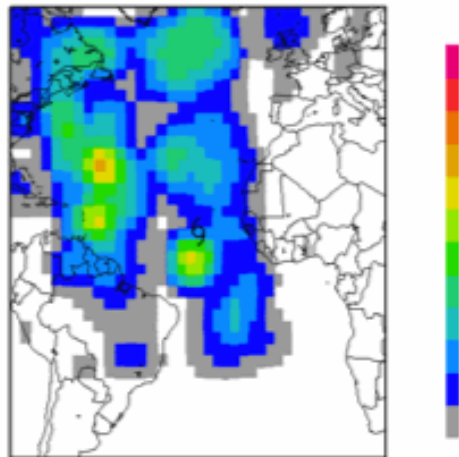
# Hurricane Fred (2009): Assimilation of all-sky SEVIRI and AIRS SFOV (q,T) in HWRF outer domain

Information content - DFS

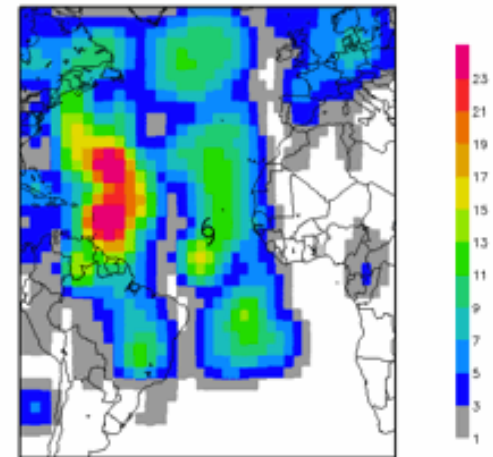
**MSG SEVIRI  
only**



**MSG SEVIRI  
and AIRS q  
profile**



**MSG SEVIRI  
and AIRS T  
profile**



In outer domain (with less clouds) DFS shows more benefit from AIRS SFOV temperature data than from specific humidity data

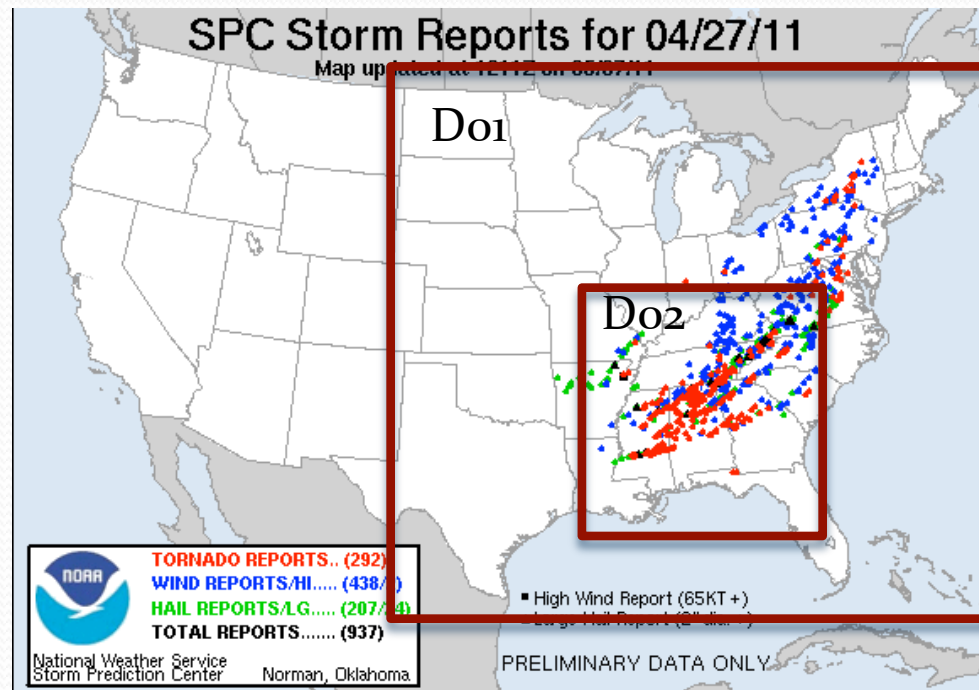


# Lightning data assimilation: Severe weather applications

- **Model:** NOAA WRF-NMM (27km/9km)
- **Results for the inner nest at 9 km resolution**
- **Observations:** WWLLN [proxy for GOES-R GLM)
- **Data assimilation interval:** 6 hours
- **Number of ensembles:** 32
- **Tornado outbreak over Southeast US in April 2011**
- From Apodaca et al. (2013)

# Severe weather outbreak over the southeastern US on April 25-18, 2011

Model domain and tornado reports for April 27, 2011

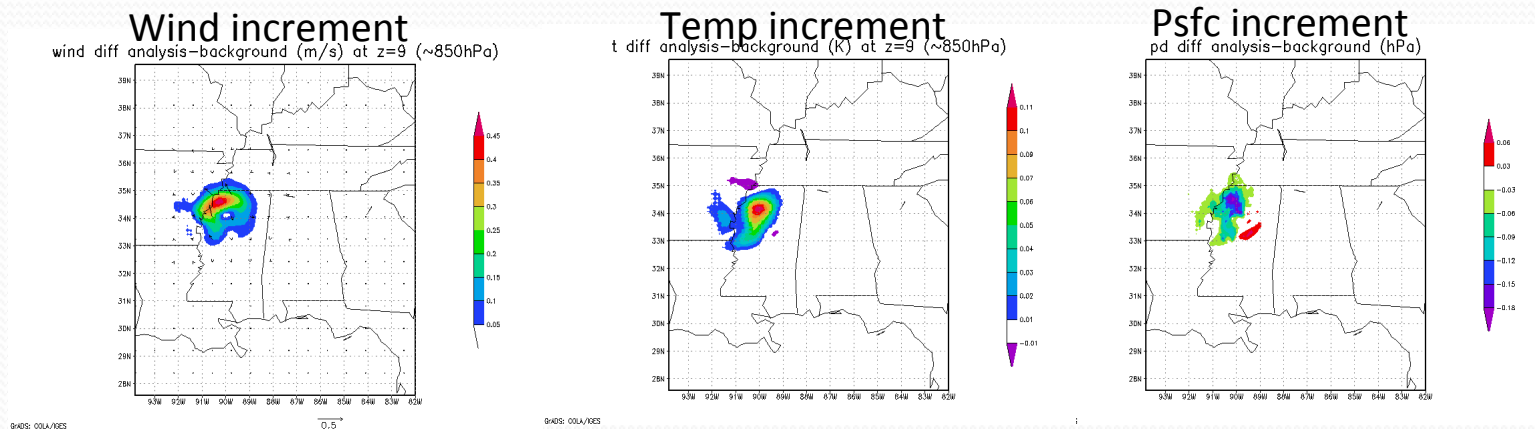


# Lightning observation operator

- **WWLLN can observe only cloud-to-ground (C-G) flashes**
- **Regression between lightning flash rate and model variables**
  - Best regression suggests cloud ice and vertical graupel flux (McCaul et al. 2009)
- **WRF-NMM microphysics (Ferrier) does not predict cloud ice:**
  - Need to rely on less accurate regression: maximum vertical updraft
- **Present:**
  - Use max vertical updraft and WWLLN
- **Future:**
  - Include more complex microphysics to improve obs operator
  - Use better GLM proxy observations (C-G and intra-cloud)
  - Increase the resolution to 1-3 km

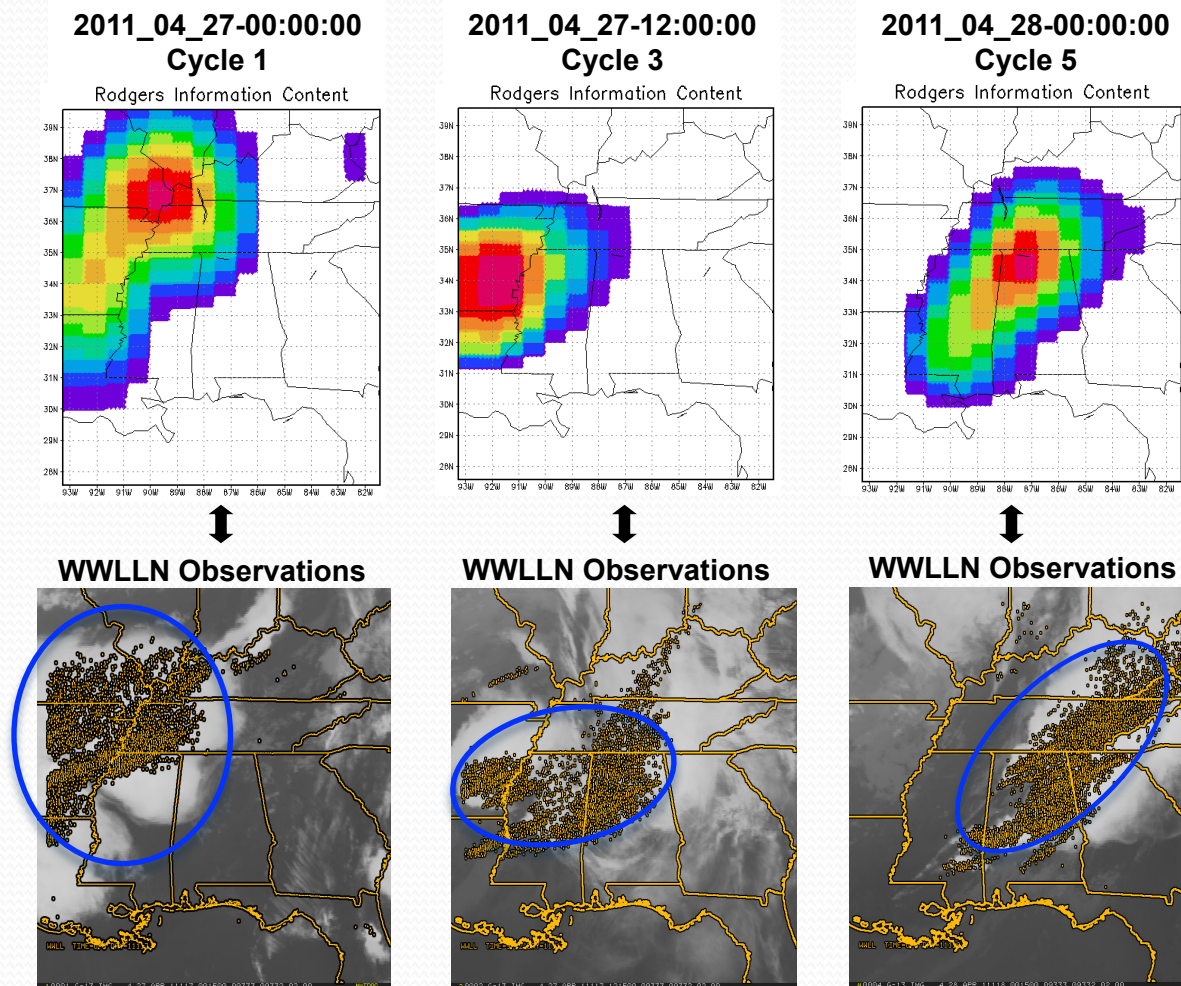
# Lightning data assimilation with MLEF: Single observation experiment

**Analysis response to a single observation of flash rate in a 6-hour interval**



**Assimilation of lightning observations impacts all model variables  
and improves storm environment conditions**

# Information content of lightning observations: DFS



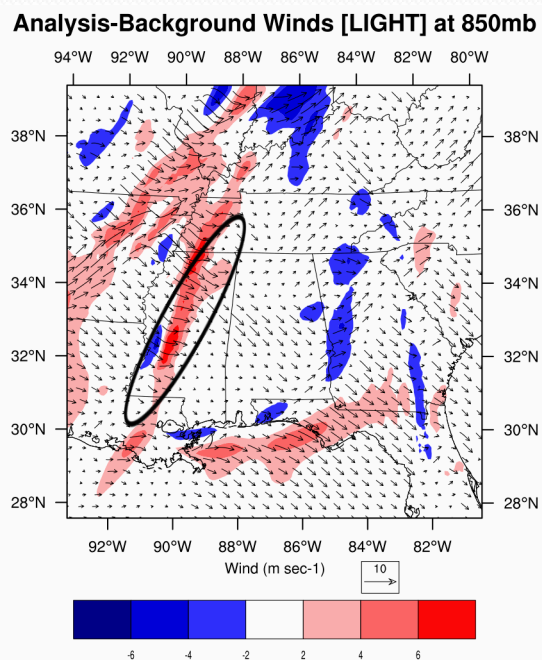
Time and flow dependent information added by assimilating lightning data



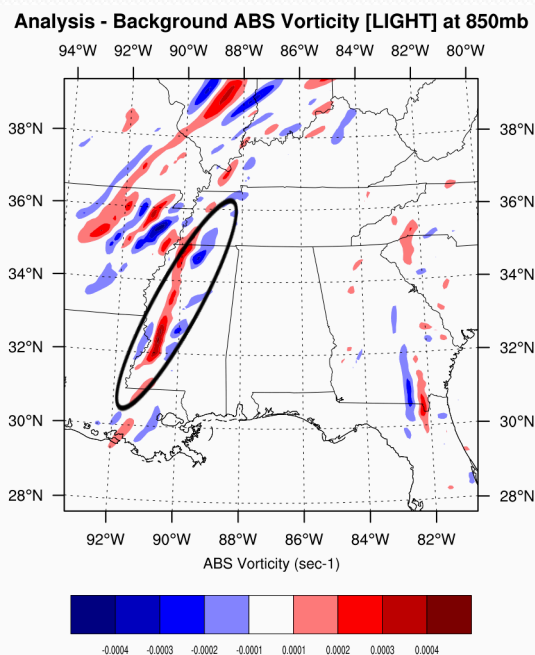
# Impact on storm environment

Analysis increments:  $x^a - x^f$

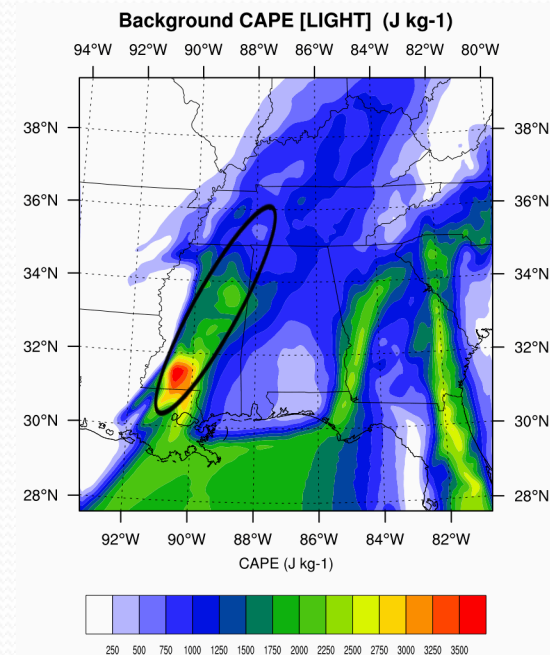
**Wind increment at 850 hPa**  
Valid 04/28 at 00UTC



**Vorticity increment at 850 hPa**  
Valid 04/28 at 00UTC



**Background CAPE**  
Valid 04/28 at 00UTC



Lightning data assimilation increases the advection of low-level vorticity into the region of large CAPE

# New direction: High-impact weather

- **Combine all observations in applications to TC/severe weather:**
  - All-sky infrared radiances(GOES-R ABI)
  - Lightning (GOES-R GLM)
  - All-sky microwave radiances
  - AIRS/IASI (sounder)
  - NOAA operational observations (GSI)
- **Examine the impact of WV channels for TC genesis**
- **Assess the value of combined observations in regional hybrid GSI**

# New directions: Coupled models



- **Extend utility of GOES-R data to chemistry:**
  - Improve predictions of high-impact weather **and** air-quality
  - WRF-CHEM model: coupled atmosphere-chemistry
  - All-sky ABI radiances and GLM flash rates contain a valuable information about NO<sub>x</sub>, O<sub>3</sub>, and aerosols
- **Extend utility of GOES-R data to land-surface and coastal ocean**
  - Focus on improving predictions of hurricane landfall, storm surge
  - coupled atmosphere-ocean-land-hydrology model
  - add ocean observations (HF radar, Lagrangian data, altimeter, satellite)



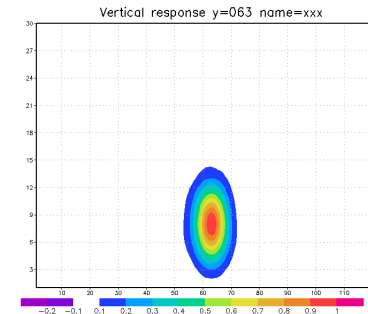
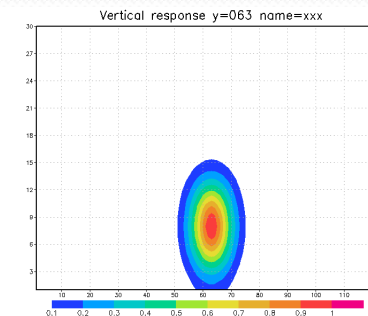
# New directions: Hybrid DA

- Extend MLEF to include static/variational and ensemble error covariances
  - Hybrid ensemble-variational error covariance
  - A single DA system (no separate variational and ensemble algorithms)
  - Maintain optimal Hessian preconditioning (e.g., observation component)
  - Requirement: Approximate variational covariance

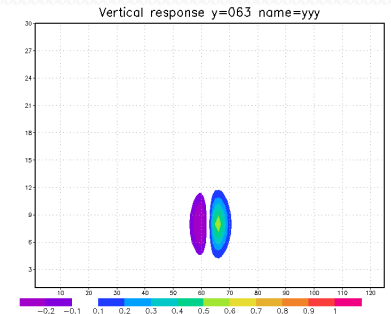
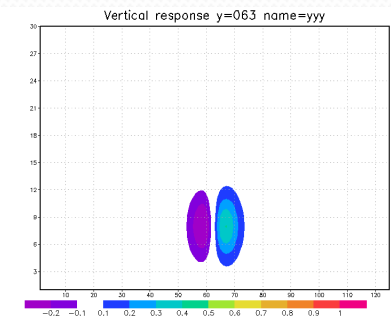
$$P_f^{1/2} = \begin{bmatrix} P_{ens}^{1/2} & P_{SR}^{1/2} \end{bmatrix} = \begin{array}{c|c} \text{ens} & \text{static} \\ \hline \text{True static} & \text{MLEF static} \end{array}$$

- Improve robustness of the system
- Efficient use of all observations

Variable 1



Variable 2



# Future



- **Continue high-impact weather DA applications**
  - Increase resolution to 1-3 km
  - Assimilate all available observations
- **Prepare for GOES-R launch**
  - simultaneous assimilation of ABI and GLM
  - use GSI/hybrid GSI as a framework to access observations
- **Expand applications to chemistry, land-surface, carbon, ocean**
  - important new applications
  - extend the utility of GOES-R data
- **Further development of hybrid variational-ensemble systems**
  - hybrid forecast error covariance with optimal Hessian preconditioning



# Thank you!

## References:

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